

## CHAPTER 1 - GRAPHING PARAMETRIC EQUATIONS

### Casio fx-CG50

Use technology to plot  $\{(x, y) \mid x = 2 \cos t, y = 3 \sin t - 2 \cos t, 0 \leq t \leq 2\pi\}$ .

Select **Graph** from the Main Menu, and press **F3** (TYPE), **F3** (Param).

Enter  $2 \cos t$  into **Xt1**, and  $3 \sin t - 2 \cos t$  into **Yt1**.

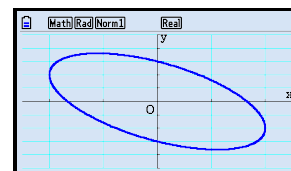
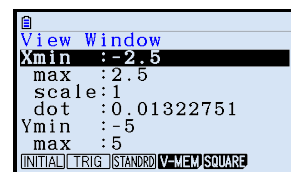
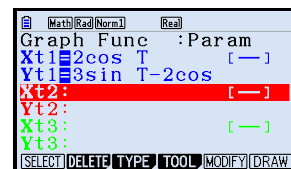
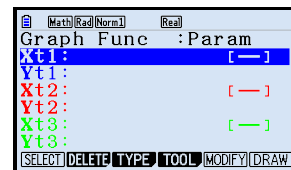
**Note:**  $t$  is entered by pressing **X,  $\theta$ , T**.

Press **SHIFT** **F3** (V-WIN) to adjust the size of the viewing window.

We set **Xmin** = -2.5, **Xmax** = 2.5, **Ymin** = -5, and **Ymax** = 5.

Make sure that **T $\theta$ min** = 0, and **T $\theta$ max** =  $2\pi$ .

Press **EXIT** to return, and press **F6** (DRAW) to plot the graph.

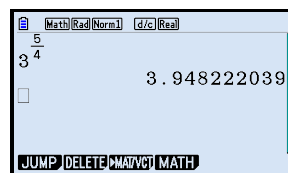


## CHAPTER 2 - CALCULATING RATIONAL EXPONENTS

### Casio fx-CG50

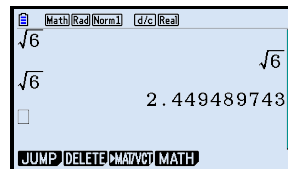
Exponents are calculated using  $\wedge$ .

To find  $3^{\frac{5}{4}}$ , enter  $3 \wedge 5 \div 4$   $\text{EXE}$ .



Square roots are calculated by pressing  $\text{SHIFT}$   $x^2$  ( $\sqrt{\phantom{x}}$ ).

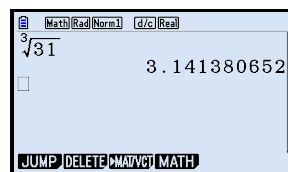
To find  $\sqrt{6}$ , press  $\text{SHIFT}$   $x^2$  ( $\sqrt{\phantom{x}}$ ) 6  $\text{EXE}$ .



**Note:** Pressing  $\text{S} \leftrightarrow \text{D}$  switches between exact and decimal expressions (where possible).

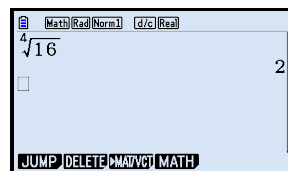
Cube roots are calculated by pressing  $\text{SHIFT}$   $(\sqrt[3]{\phantom{x}})$ .

To find  $\sqrt[3]{31}$ , press  $\text{SHIFT}$   $(\sqrt[3]{\phantom{x}})$  31  $\text{EXE}$ .



Higher roots are calculated by pressing  $\text{SHIFT}$   $\wedge$  ( $\sqrt[n]{\phantom{x}}$ ).

To find  $\sqrt[4]{16}$ , enter  $4 \text{SHIFT} \wedge (\sqrt[n]{\phantom{x}})$  16  $\text{EXE}$ .

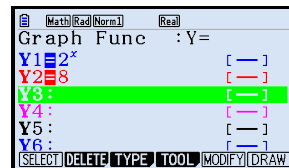


## CHAPTER 2 - EXPONENTIAL EQUATIONS

### Casio fx-CG50

To solve the equation  $2^x = 8$ , we find the point of intersection of the graphs  $y = 2^x$ , and  $y = 8$ .

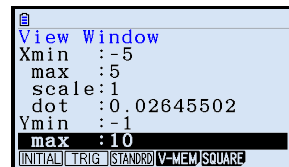
Select **Graph** from the Main Menu, then store  $2^x$  into **Y1**, and 8 into **Y2**.



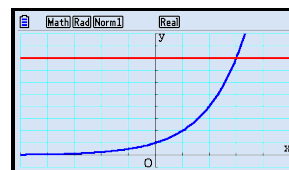
Press **SHIFT** **F3** (**V-WIN**) to adjust the size of the viewing window.

We set **Xmin** = -5, **Xmax** = 5, **Ymin** = -1, and **Ymax** = 10.

**Note:** The viewing window should show the point of intersection.



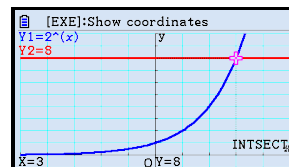
Press **F6** (**DRAW**) to draw the graphs of the functions.



To find the point of intersection, press **F5** (**G-SOLVE**), then **F5** (**INTSECT**).

The graphs intersect at (3, 8).

So, the solution to  $2^x = 8$  is  $x = 3$ .



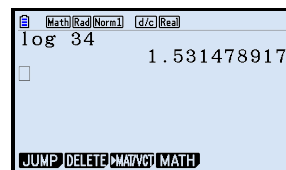
## CHAPTER 3 - LOGARITHMS IN BASE 10

### Casio fx-CG50

We can perform operations involving logarithms in base 10 using the **log** button.

To evaluate  $\log 34$ , press **log** 34 **EXE**.

So,  $\log 34 \approx 1.53$ .



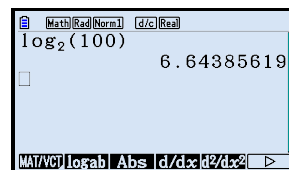
## CHAPTER 3 - LOGARITHMS IN BASE $a$

### Casio fx-CG50

We can perform operations involving logarithms in base  $a$  using the **logab** function.

To find  $\log_2 100$ , press **F4** (**MATH**), **F2** (**logab**), then 2 **▶** 100 **EXE**.

So,  $\log_2 100 \approx 6.64$ .



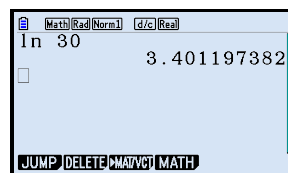
## CHAPTER 3 - NATURAL LOGARITHMS

### Casio fx-CG50

We can perform operations involving natural logarithms using the **ln** button.

To evaluate  $\ln 30$ , press **ln** 30 **EXE**.

So,  $\ln 30 \approx 3.40$ .



## CHAPTER 3 - GRAPHING LOGARITHMIC FUNCTIONS

### Casio fx-CG50

To draw the graph of the function  $f(x) = \log_2(x - 1) + 1$ , first select **Graph** from the Main Menu.

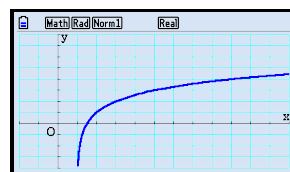
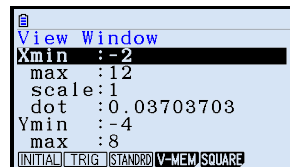
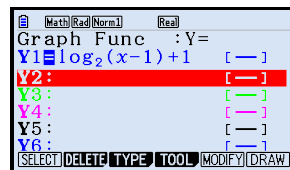
To enter  $\log_2(x - 1) + 1$  into **Y1**, press **OPTN**, **F2** (CALC), then **F4** (logab).

Then press 2 **X,  $\theta$ , T** **-** 1 **+** 1 **EXE**.

Press **SHIFT** **F3** (V-WIN) to adjust the viewing window.

We set **Xmin** = -2, **Xmax** = 12, **Ymin** = -4, and **Ymax** = 8.

Press **EXE**, then **F6** (DRAW) to graph the function.



## CHAPTER 4 - OPERATIONS WITH COMPLEX NUMBERS

### Casio fx-CG50

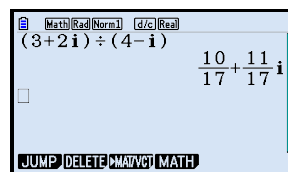
The imaginary number  $i$  is entered by pressing **SHIFT** **0** ( $i$ ).

For example, suppose  $z = 3 + 2i$ , and  $w = 4 - i$ .

To calculate  $\frac{z}{w}$ , enter  $(3 + 2i) \div (4 - i)$ , then press **EXE**.

**Note:** Press **S  $\leftrightarrow$  D** to display the answer in fractional form.

So,  $\frac{z}{w} = \frac{10}{17} + \frac{11}{17}i$ .





## CHAPTER 6 - SOLVING MODULUS EQUATIONS

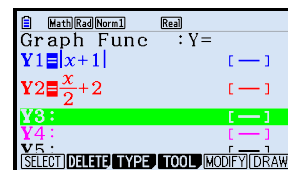
### Casio fx-CG50

To solve  $|x + 1| = \frac{x}{2} + 2$  graphically, we find the intersection points of the graphs  $y = |x + 1|$ , and  $y = \frac{x}{2} + 2$ .

First select **Graph** from the Main Menu.

Enter  $|x + 1|$  into **Y1**, and  $\frac{x}{2} + 2$  into **Y2**.

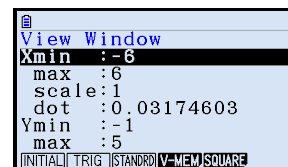
**Note:** To enter modulus functions, we use the **Abs** function which we access by pressing **OPTN** **F5** (NUMERIC), **F1** (Abs).



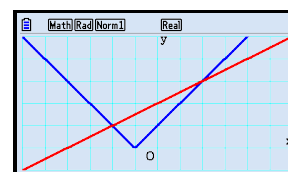
Press **SHIFT** **F3** (V-WIN) to adjust the size of the viewing window.

We set **Xmin** = -6, **Xmax** = 6, **Ymin** = -1, and **Ymax** = 5.

**Note:** The viewing window should show the points of intersection.



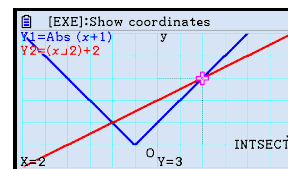
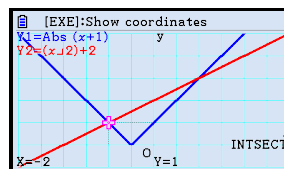
Press **EXE** to return, and press **F6** (DRAW) to plot the graphs.



To find the points of intersection, press **F5** (G-Solv), **F5** (INTSECT), and use **◀** **▶** to move between the points of intersection.

The graphs intersect at  $(-2, 1)$  and  $(2, 3)$ .

So, the solutions to  $|x + 1| = \frac{x}{2} + 2$  are  $x = -2$  or  $2$ .



## CHAPTER 6 - SOLVING MODULUS INEQUALITIES

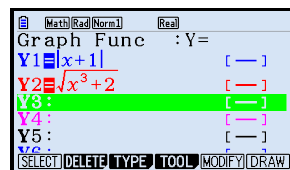
### Casio fx-CG50

To solve  $|x + 1| > \sqrt{x^3 + 2}$  graphically, we find the intersection points of the graphs  $y = |x + 1|$ , and  $y = \sqrt{x^3 + 2}$ .

First select **Graph** from the Main Menu.

Enter  $|x + 1|$  into **Y1**, and  $\sqrt{x^3 + 2}$  into **Y2**.

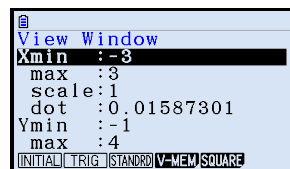
**Note:** To enter modulus functions, we use the **Abs** function which we access by pressing **OPTN** **F5** (NUMERIC), **F1** (Abs).



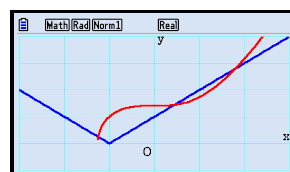
Press **SHIFT** **F3** (V-WIN) to adjust the size of the viewing window.

We set **Xmin** = -3, **Xmax** = 3, **Ymin** = -1, and **Ymax** = 4.

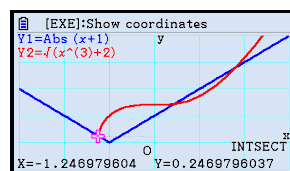
**Note:** The viewing window should show the points of intersection.



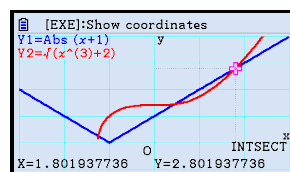
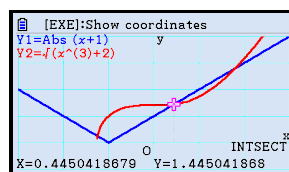
Press **EXE** to return, and press **F6** (DRAW) to plot the graphs.



To find the points of intersection, press **F5** (G-Solv), **F5** (INTSECT).



Use **◀** **▶** to move between the points of intersection.



The graphs intersect at  $x \approx -1.2470$ ,  $x \approx 0.4450$ , and  $x \approx 1.8019$ .

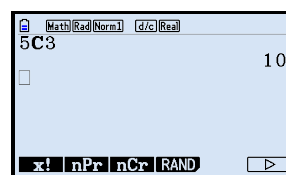
So,  $|x + 1| > \sqrt{x^3 + 2}$  when  $-\sqrt[3]{2} \leq x < -1.247$  and when  $0.445 < x < 1.802$ .

## CHAPTER 7 - COMBINATIONS

### Casio fx-CG50

To find  $\binom{5}{3}$ , press 5 **OPTN** **F6** ( $\triangleright$ ) **F3** (PROB) **F3** (nCr) 3 **EXE**.

So,  $\binom{5}{3} = 10$ .

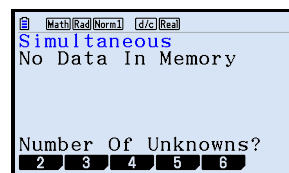


## CHAPTER 11 - SOLVING SYSTEMS OF LINEAR EQUATIONS

### Casio fx-CG50

To solve systems of linear equations, select **Equation** from the Main menu, and press

**F1** (SIMUL).

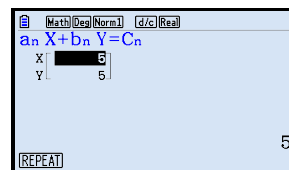
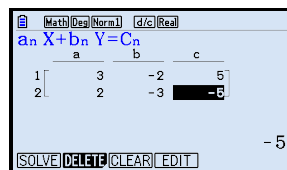


### Unique solution

Consider the following system of linear equations: 
$$\begin{cases} 3x - 2y = 5 \\ 2x - 3y = -5 \end{cases}$$

Press **F1** (2) to select 2 unknowns, and set up the screen as shown.

Press **F1** (SOLVE) to view the results.



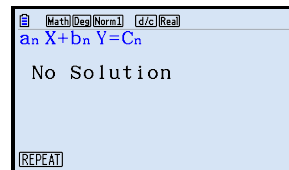
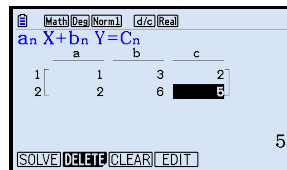
So,  $x = 5$ ,  $y = 5$ .

### No solution

Consider the following system of linear equations: 
$$\begin{cases} x + 3y = 2 \\ 2x + 6y = 5 \end{cases}$$

Press **F1** (2) to select 2 unknowns, and set up the screen as shown.

Press **F1** (SOLVE) to view the results.



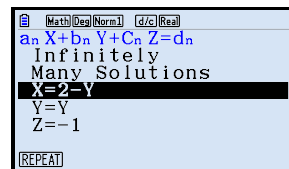
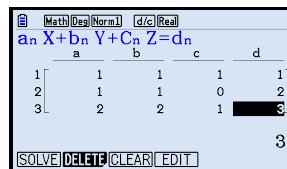
So, the system has no solutions.

### Infinitely many solutions

Consider the following system of linear equations: 
$$\begin{cases} x + y + z = 1 \\ x + y = 2 \\ 2x + 2y + z = 3 \end{cases}$$

Press **F2** (3) to select 3 unknowns, and set up the screen as shown.

Press **F1** (SOLVE) to view the results.



So, letting  $y = t$  we get  $x = 2 - t$ ,  $y = t$ ,  $z = -1$ ,  $t \in \mathbb{R}$ .

## CHAPTER 14 - CONVERTING BETWEEN POLAR AND CARTESIAN FORM

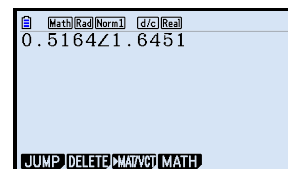
### Casio fx-CG50

Select **Run-Matrix** from the Main Menu. Press **SHIFT** **MENU** (SET UP), and ensure that **Angle** is set to **Rad**. Press **EXIT** to return.

### Polar to Cartesian form

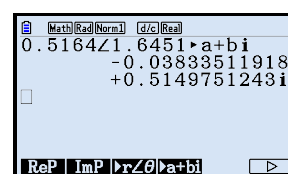
Enter complex numbers in polar form using the angle function  $\angle$ .

For example, to input  $0.5164 \operatorname{cis}(1.6451)$ , enter  $0.5164$  **SHIFT** **X,  $\theta$ , T** ( $\angle$ )  $1.6451$ .



To convert complex numbers in polar form to Cartesian form, use the **►a+bi** function.

For example, to convert  $0.5164 \operatorname{cis}(1.6451)$  to Cartesian form, enter  $0.5164 \operatorname{cis}(1.6451)$ , then press **OPTN** **F3** (COMPLEX), **F6** ( $\triangleright$ ), **F4** (**►a+bi**), then **EXE**.



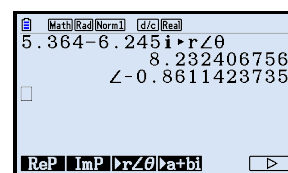
So,  $0.5164 \operatorname{cis}(1.6451) \approx -0.0383 + 0.515i$ .

### Cartesian to polar form

To convert complex numbers in Cartesian form to polar form, use the **►r∠θ** function.

For example, to convert  $5.364 - 6.245i$  to polar form, first enter  $5.364 - 6.245i$ , then press **OPTN** **F3** (COMPLEX), **F6** ( $\triangleright$ ), **F3** (**►r∠θ**), then **EXE**.

**Note:**  $i$  is entered by pressing **SHIFT** **0** ( $i$ ).



So,  $5.364 - 6.245i \approx 8.23 \operatorname{cis}(-0.861)$ .

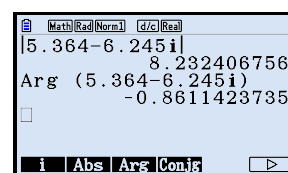
Alternatively, the modulus and argument may be calculated separately using the **Abs** and **Arg** functions.

To find the modulus, press **OPTN** **F3** (COMPLEX), **F2** (Abs).

Enter  $5.364 - 6.245i$ , then press **EXE**.

To find the argument, press **OPTN** **F3** (COMPLEX), **F3** (Arg).

Enter  $5.364 - 6.245i$ , then press **EXE**.



So,  $|5.364 - 6.245i| \approx 8.23$ , and  $\arg(5.364 - 6.245i) \approx -0.861$ .

$\therefore 5.364 - 6.245i \approx 8.23 \operatorname{cis}(-0.861)$ .

**Note:** The calculator has a **Complex Mode** setting, accessed by pressing **SHIFT** **MENU** (SET UP).

When set to **a+bi**, complex numbers in polar form are converted to Cartesian form after pressing **EXE**.

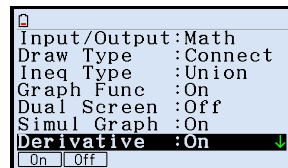
When set to **r∠θ**, complex numbers in Cartesian form are converted to polar form after pressing **EXE**.

## CHAPTER 16 - GRADIENT OF A TANGENT

### Casio fx-CG50

To find the gradient of the tangent to  $y = x^2$  when  $x = 2$ , we first select **Graph** from the Main Menu.

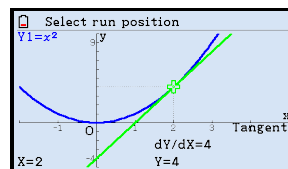
Press **SHIFT** **MENU** (SET UP), and make sure the **Derivative** setting is **On**.



Draw the graph of  $y = x^2$ , then press **SHIFT** **F4** (SKETCH) **F2** (Tangent).

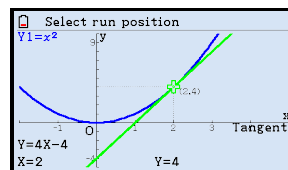
Press 2 **EXE**.

We can see that the tangent has a gradient of 4 at this point.



Press **EXE** again to find the equation of the tangent.

The tangent has equation  $y = 4x - 4$ .



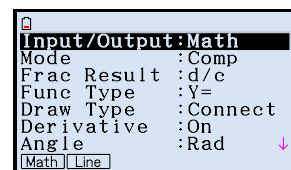
## CHAPTER 20 - ESTIMATING AREA USING RECTANGLES

### Casio fx-CG50

To calculate the lower and upper sums for the area between the graph of  $y = x^2$  and the  $x$ -axis on the interval  $0 \leq x \leq 1$  using 4 equal subdivisions, select **Run-Matrix** from the Main Menu.

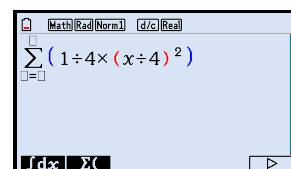
Press **SHIFT** **MENU** (SET UP) and make sure **Input/Output** is set to **Math**.

Then press **EXIT**.



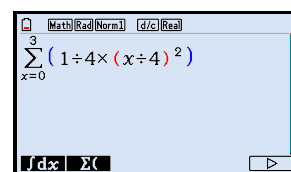
Press **F4** (MATH), **F6** ( $\triangleright$ ), **F2** ( $\sum()$ ) to insert a sum operator.

Enter the expression  $(1 \div 4) \times (x \div 4)^2$ .

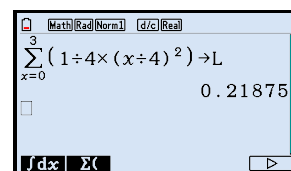


We will first calculate the lower sum.

Press **▶** **X,  $\theta$ , T** **▶** 0 **▶** 3 to indicate that  $x$  ranges from 0 to 3.

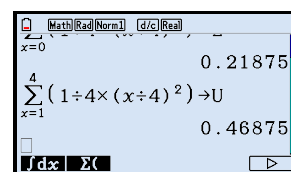


Press **▶** **→** **ALPHA** **→** (**L**) followed by **EXE** to calculate the lower sum and store it in the variable **L**.

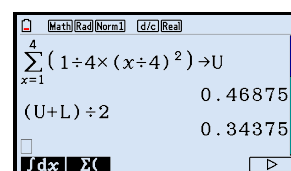


We can repeat this process to calculate the upper sum.

The only difference is that  $x$  ranges from 1 to 4 instead of 0 to 3 and we store the result in a different variable **U**.



Finally, calculate the average of the upper and lower sums  $(U + L) \div 2$  to obtain an estimate of the area.



**Note:** You should be able to adapt these instructions to calculate lower and upper sums for different values of  $n$  (the number of subdivisions).

## CHAPTER 20 - DEFINITE INTEGRALS

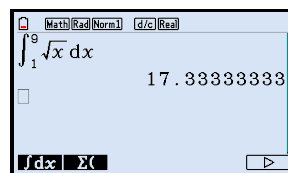
### Casio fx-CG50

To find  $\int_1^9 \sqrt{x} \, dx$ , select **Run-Matrix** from the Main Menu, and press **F4** (**MATH**),

**F6** (**▷**), **F1** ( $\int \, dx$ ).

Set up the screen as shown and press **EXE**.

So,  $\int_1^9 \sqrt{x} \, dx = 17\frac{1}{3}$ .





## CHAPTER 22 - EVALUATING DEFINITE INTEGRALS

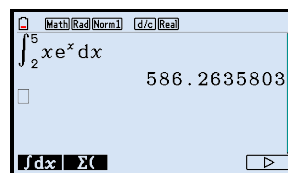
### Casio fx-CG50

To find  $\int_2^5 x e^x dx$ , select **Run-Matrix** from the Main Menu, and press **F4** (**MATH**) **F6** (**▷**) **F1** ( $\int dx$ ).

Set up the screen as shown and press **EXE**.

**Note:**  $e$  is accessed by pressing **SHIFT** **ln** ( $e^x$ ).

So,  $\int_2^5 x e^x dx \approx 586.3$ .

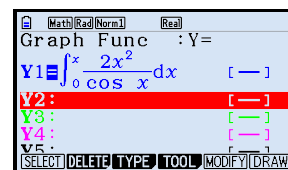


## CHAPTER 22 - SOLVING EQUATIONS WITH DEFINITE INTEGRALS

### Casio fx-CG50

To solve  $\int_0^a 2x^2 \sec x \, dx = \frac{2}{5}$ ,  $0 < a < 1$  directly using technology, select **Graph** from the Main Menu.

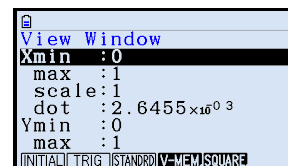
Enter  $\int_0^x 2x^2 \sec x \, dx$  into **Y1**.



**Note:** To enter the integral sign, press **OPTN** **F2** (**CALC**), then **F3** ( $\int dx$ ).

To enter  $\sec x$ , we enter  $\frac{1}{\cos x}$ .

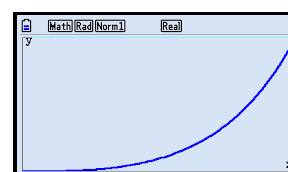
Press **SHIFT** **F3** (**V-WIN**) to adjust the viewing window.



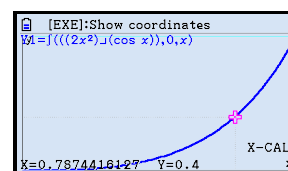
We set **Xmin** = 0, **Xmax** = 1, **Ymin** = 0, and **Ymax** = 1.

**Note:** Ensure that the viewing window does not include any asymptotes of the function you are integrating.

Press **EXIT**, then **F6** (**DRAW**) to draw the graph.



Press **SHIFT** **F5** (**G-SOLVE**), **F6** (**>**), then press **F2** (**X-CAL**).



Enter  $\frac{2}{5}$  then press **EXE** to find the value of  $a$  such that  $\int_0^a 2x^2 \sec x \, dx = \frac{2}{5}$ .

So,  $a \approx 0.787$ .

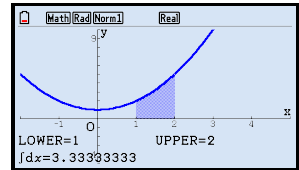
## CHAPTER 22 - AREA UNDER CURVES

### Casio fx-CG50

To find the area enclosed by  $y = x^2 + 1$ , the  $x$ -axis,  $x = 1$ , and  $x = 2$ , we first draw the graph of  $y = x^2 + 1$ .

Press **F5** (**G-SOLVE**) **F6** (**▷**) **F3** (**∫ dx**) **F1** (**∫ dx**) to select the integral tool.

Press 1 **EXE** 2 **EXE** to specify the lower and upper bounds of the integral.



So, the area of the region is  $3\frac{1}{3}$  units<sup>2</sup>.

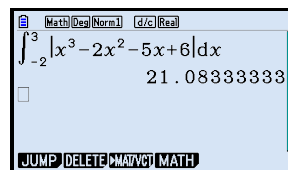
## CHAPTER 22 - FINDING THE AREA ENCLOSED BY A CURVE AND THE $x$ -AXIS

### Casio fx-CG50

To find  $\int_{-2}^3 |x^3 - 2x^2 - 5x + 6| dx$ , start by selecting **Run-Matrix** from the Main Menu.

Press **F4** (**MATH**), **F6** ( $\triangleright$ ), **F1** ( $\int dx$ ) to access the integral template.

Set up the screen as shown, then press **EXE**.



**Note:** To access the modulus function, press **OPTN** **F6** ( $\triangleright$ ), **F4** (**NUMERIC**), **F1** (**Abs**).

So,  $\int_{-2}^3 |x^3 - 2x^2 - 5x + 6| dx \approx 21.1$ .

## CHAPTER 22 - VOLUMES OF REVOLUTION

### Casio fx-CG50

The volume of the solid formed when the graph of the function  $y = x^2$  for  $0 \leq x \leq 5$  is revolved through  $2\pi$  about the  $x$ -axis, is given by  $\pi \int_0^5 x^4 dx$ .

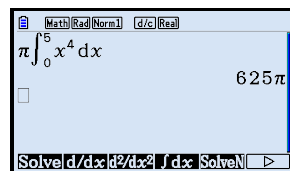
To evaluate this integral, first select **Run-Matrix** from the Main Menu.

Enter the expression as shown alongside, and press **EXE**.

**Note:**  $\pi$  is entered by pressing **SHIFT**  **$\times 10^x$**  ( $\pi$ ).

To enter the integral sign, press **OPTN** **F4** (**CALC**), then **F4** ( $\int dx$ ).

So, volume of revolution =  $625\pi$  units<sup>3</sup>.



## CHAPTER 24 - MACLAURIN POLYNOMIALS

### Casio fx-CG50

To obtain a Maclaurin polynomial which estimates  $e^{0.4}$  with error less than 0.000 01, we must find  $n$  such that

$$\frac{(0.4)^{n+1}}{(n+1)!} < 3.676 \times 10^{-6}.$$

First select **Table** from the Main Menu.

Enter  $\frac{(0.4)^{x+1}}{(x+1)!}$  into **Y1**.

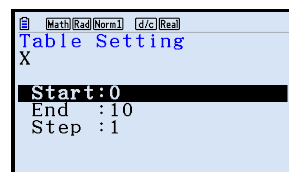
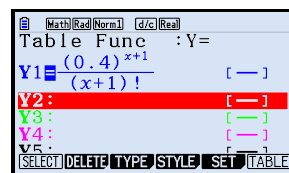
**Note:** ! is entered by pressing **OPTN** **F4** (**PROB**), then **F1** (**x!**).

Press **F5** (**SET**), set up the screen as shown, and press **EXE**.

Press **F6** (**TABLE**) to view the table of values.

The first time that **Y1** falls below  $3.676 \times 10^{-6}$  is when  $x = 6$ .

So, for  $n \geq 6$  the  $n$ th Maclaurin polynomial estimates  $e^{0.4}$  with error less than 0.000 01.



X	Y1
4	8.5E-5
5	5.0E-6
6	3.2E-7
7	1.0E-8
3.250793651 × 10 <sup>-7</sup>	

## CHAPTER 25 - EULER'S METHOD

### Casio fx-CG50

Consider the differential equation  $\frac{dy}{dx} = e^x + 1$  with  $y(0) = 1$ .

To estimate  $y(0.5)$  using Euler's method with step size 0.005, we have  $x_0 = 0$ ,  $y_0 = 1$ , and

$$\begin{cases} x_i = x_{i-1} + 0.005 \\ y_i = y_{i-1} + 0.005(e^{x_{i-1}} + 1). \end{cases}$$

Select **Recursion** from the Main Menu, press **F3** (**TYPE**), then **F2** (**a<sub>n+1</sub>**).

Enter  $a_n + 0.005$  into **a<sub>n+1</sub>**, and  $b_n + 0.005(e^{a_n} + 1)$  into **b<sub>n+1</sub>**.

**Note:**  $a_n$  is entered by pressing **F4** (**n.a<sub>n</sub>...**), then **F2** (**a<sub>n</sub>**).

$b_n$  is entered by pressing **F4** (**n.a<sub>n</sub>...**), then **F3** (**b<sub>n</sub>**).

Press **F5** (**SET**) and adjust the table settings.

Set **Start** = 0, and **End** = 100 since we are taking  $\frac{0.5}{0.005} = 100$  steps.

Set **a<sub>0</sub>** = 0 since  $x_0 = 0$ , and **b<sub>0</sub>** = 1 since  $y_0 = 1$ .

Press **EXIT**, then **F6** (**TABLE**) to view the table of values.

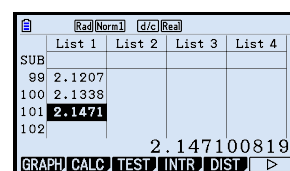
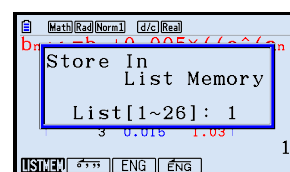
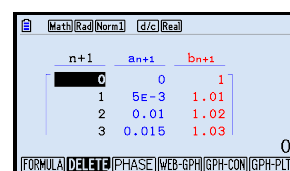
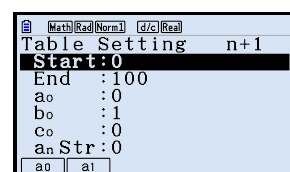
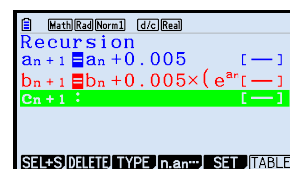
Press **▶▶** to highlight the first entry in the **b<sub>n+1</sub>** column.

Press **OPTN** **F1** (**LISTMEM**), then enter 1 **EXE** to save the values of **b<sub>n+1</sub>** into **List 1**.

To view **List 1** press **MENU** and select **Statistics**.

Press **▲** until the 101st entry is shown.

So,  $y(0.5) \approx 2.1471$ .



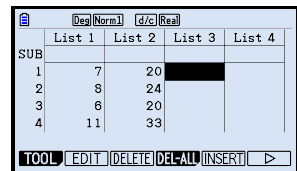
## CHAPTER 26 - DRAWING SCATTER DIAGRAMS

### Casio fx-CG50

Draw a scatter diagram of the following data set:

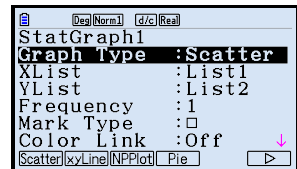
$x$	7	8	6	11	6	4	5
$y$	20	24	20	33	18	10	13

Enter the  $x$ -values into **List 1** and the  $y$ -values into **List 2**.



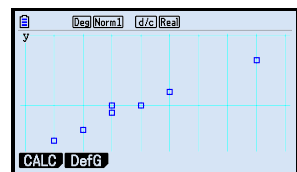
	List 1	List 2	List 3	List 4
1	7	20		
2	8	24		
3	6	20		
4	11	33		

Press **F1** (**GRAPH**), **F6** (**SET**), and set up **StatGraph1** as shown.



StatGraph1
Graph Type : Scatter
XList : List1
YList : List2
Frequency : 1
Mark Type : [ ]
Color Link : Off
Scatter   kylLine   NPPlot   Pie

Press **EXIT**, then **F1** (**GRAPH1**) to draw the scatter diagram.





## CHAPTER 26 - CALCULATING $r$

### Casio fx-CG50

Find the correlation coefficient  $r$  for the data alongside.

$x$	2	5	6	3	9
$y$	11	6	4	6	3

Enter the  $x$ -values into **List 1**, and the  $y$ -values into **List 2**.

	List 1	List 2	List 3	List 4
SUB				
1	2	11		
2	5	6		
3	6	4		
4	3	6		

Press **F2** (CALC), **F6** (SET), and set up the screen as shown alongside.

	List 1	List 2	List 3	List 4
1Var XList	:List1			
1Var Freq	:1			
2Var XList	:List1			
2Var YList	:List2			
2Var Freq	:1			

Press **EXIT**, **F3** (REG), **F1** (X), then **F1** (ax+b).

	List 1	List 2	List 3	List 4
LinearReg(ax+b)				
a	= -0.96666666			
b	= 10.83333333			
r	= -0.8589058			
r <sup>2</sup>	= 0.73771929			
MSe	= 3.32222222			
y=ax+b				

So,  $r \approx -0.859$ .

## CHAPTER 26 - REGRESSION LINE

### Casio fx-CG50

Find the regression line for the data alongside.

$x$	55	36	25	47	60	64	42	50
$y$	120	90	60	160	190	250	110	150

Enter the  $x$ -values into **List 1**, and the  $y$ -values into **List 2**.

	List 1	List 2	List 3	List 4
SUB				
1	55	120		
2	36	90		
3	25	60		
4	47	160		

GRAPH CALC TEST INTR DIST

Press **F2** (CALC), **F6** (SET), and set up the screen as shown alongside.

	Var	YList	Freq
1Var	XList	List1	1
2Var	XList	List1	
2Var	YList	List2	
2Var	Freq	1	

LIST

Press **EXIT**, **F3** (REG), **F1** (X), then **F1** (ax+b).

	Var	YList	Freq
1Var	XList	List1	1
2Var	XList	List1	
2Var	YList	List2	
2Var	Freq	1	

LinearReg(ax+b)  
 $a = 4.17825196$   
 $b = -56.694686$   
 $r = 0.89484388$   
 $r^2 = 0.80074556$   
 $MSe = 839.7744$   
 $y = ax + b$

COPY

So, the regression line is  $y \approx 4.18x - 56.7$ .

## CHAPTER 26 - REGRESSION LINE ON A SCATTER DIAGRAM

### Casio fx-CG50

Plot the regression line on the scatter diagram of the data below:

$x$	55	36	25	47	60	64	42	50
$y$	120	90	60	160	190	250	110	150

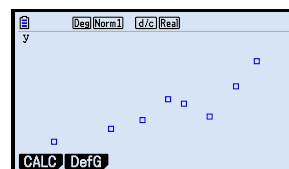
First enter the  $x$ -values into **List 1**, and the  $y$ -values into **List 2**.

	List 1	List 2	List 3	List 4
SUB				
1	55	120		
2	36	90		
3	25	60		
4	47	160		

Press **F1** (**GRAPH**), **F6** (**SET**), and set up **StatGraph1** as shown.

	StatGraph1
Graph Type	: Scatter
XList	: List1
YList	: List2
Frequency	: 1
Mark Type	: □
Color Link	: Off

Press **EXIT**, then **F1** (**GRAPH1**) to draw a scatter diagram of the data.

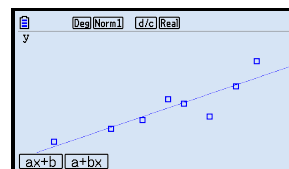


Press **F1** (**CALC**), **F2** (**X**), **F1** (**ax+b**) to perform a linear regression on the data.

So, the regression line is  $y \approx 4.18x - 56.7$ .

	LinearReg(ax+b)
a	= 4.17825196
b	= -56.694686
r	= 0.89484388
r <sup>2</sup>	= 0.80074556
MSe	= 839.7744
y	= ax + b

Press **F6** (**DRAW**) to plot the regression line on the scatter diagram.



## CHAPTER 27 - STANDARD DEVIATION OF A DISCRETE RANDOM VARIABLE

### Casio fx-CG50

Find the standard deviation of the probability distribution alongside.

$x_i$	1	2	3	4	5
$p_i$	0.23	0.38	0.21	0.13	0.05

To find the standard deviation, first select **Statistics** from the Main Menu, enter the values for  $x_i$  into **List 1**, and the values for  $p_i$  into **List 2** as shown.

	List 1	List 2	List 3	List 4
SUB				
1	1	0.23		
2	2	0.38		
3	3	0.21		
4	4	0.13		

Press **F6** ( $\triangleright$ ) until the **GRAPH** icon is in the bottom left corner of the screen, then press **F2** (CALC), **F6** (SET), and make sure the screen is set up as shown.

1Var	XList	:List1
1Var	Freq	:List2
2Var	XList	:List1
2Var	YList	:List2
2Var	Freq	:1

Press **EXIT**, then **F1** (1-VAR) to view the statistics.

1-Variable	
$\bar{x}$	=2.39
$\Sigma x$	=2.39
$\Sigma x^2$	=6.97
$\sigma x$	=1.12156141
$sx$	=
$n$	=1

So,  $\sigma \approx 1.12$ .

## CHAPTER 27 - MEAN AND STANDARD DEVIATION OF A DISCRETE RANDOM VARIABLE

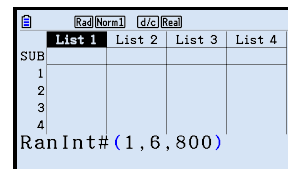
### Casio fx-CG50

Calculate the mean and standard deviation of 800 randomly generated integers between 1 and 6.

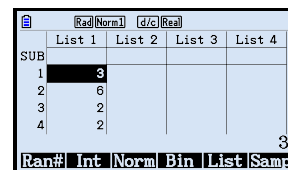
To generate random integers, use the **RandInt#** function.

First select **Statistics** from the Main Menu.

Move the cursor to highlight the header of **List 1** and press **OPTN** **F5** (**PROB**), **F4** (**RAND**), **F2** (**Int**), then 1 **,** 6 **,** 800 **)**.

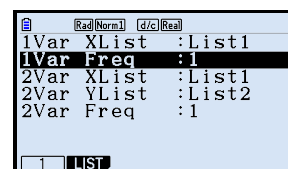


Press **EXE** to populate **List 1** with 800 random integers from 1 to 6.

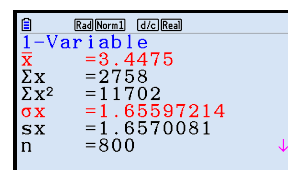


Press **SHIFT** **EXIT** (**QUIT**), **F2** (**CALC**), **F6** (**SET**).

Set up the screen as shown alongside.



Press **EXIT**, then **F1** (**1-VAR**) to view the statistics.



So,  $\mu \approx 3.45$  and  $\sigma \approx 1.66$ .

**Note:** Your values of  $\mu$  and  $\sigma$  may not be exactly the same, but should be close (within  $\pm 0.1$ ).

## CHAPTER 27 - BINOMIAL PROBABILITIES

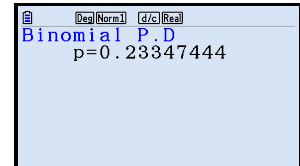
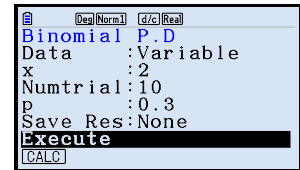
### Casio fx-CG50

To find  $P(X = 2)$  for  $X \sim B(10, 0.3)$ , select **Statistics** from the Main Menu.

Press **F5** (**DIST**), **F5** (**BINOMIAL**), then **F1** (**Bpd**).

Set up the screen as shown, then press **EXE**.

So,  $P(X = 2) \approx 0.233$ .

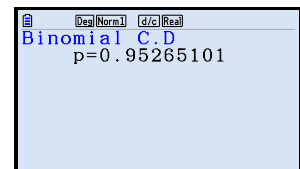
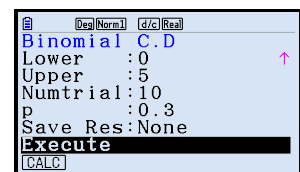


To find  $P(X \leq 5)$  for  $X \sim B(10, 0.3)$ , select **Statistics** from the Main Menu.

Press **F5** (**DIST**), **F5** (**BINOMIAL**), then **F2** (**Bcd**).

Set up the screen as shown, then press **EXE**.

So,  $P(X \leq 5) \approx 0.953$ .



## CHAPTER 27 - MEAN AND STANDARD DEVIATION OF A BINOMIAL DISTRIBUTION

### Casio fx-CG50

Calculate the mean and standard deviation for the variable  $X \sim B(30, 0.25)$ .

First enter the values 0, 1, ..., 30 into **List 1**.

Press **F5** (**DIST**), **F5** (**BINOMIAL**), **F1** (**Bpd**), set up the screen as shown, then press **EXE**.

**Note:** This calculates  $P(X = x)$  for every value of  $x$  from 0 to 30, and saves the results in **List 2**.

Press **EXIT** to return to the List screen.

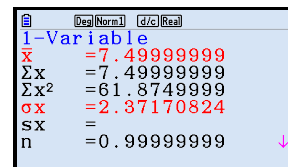
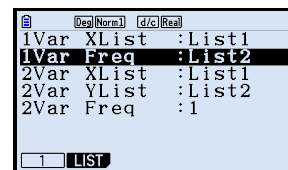
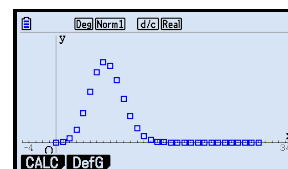
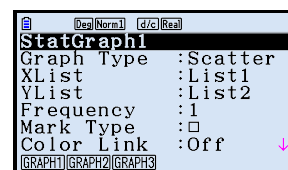
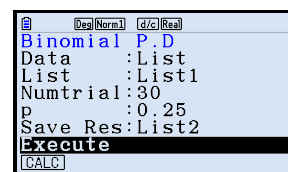
To draw a scatter plot of the data, press **F1** (**GRAPH**), **F6** (**SET**), and set up **StatGraph1** as shown.

Press **EXIT**, then **F1** (**GRAPH1**) to draw the scatter plot.

To calculate the descriptive statistics, press **SHIFT** **EXIT** (**QUIT**), **F2** (**CALC**), **F6** (**SET**), and set up the screen as shown.

Press **EXIT**, then **F1** (**1-VAR**).

So,  $\mu = 7.5$  and  $\sigma \approx 2.3717$ .



## CHAPTER 28 - FINDING THE MEAN OF A CONTINUOUS RANDOM VARIABLE

### Casio fx-CG50

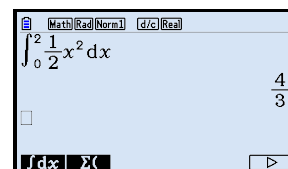
The mean of the distribution with probability density function  $f(x) = \frac{1}{2}x$ ,  $0 \leq x \leq 2$  is

$$\mu = \int_0^2 x f(x) dx = \int_0^2 \frac{1}{2} x^2 dx.$$

To evaluate this, select **Run-Matrix** from the Main Menu.

Set up the screen as shown alongside and press **EXE**.

**Note:** The integral is entered by pressing **F4** (**MATH**), **F6** (**>**), **F1** ( **$\int dx$** ).



So,  $\mu = \frac{4}{3}$ .



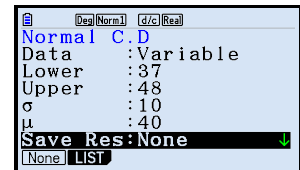
## CHAPTER 28 - NORMAL PROBABILITIES

### Casio fx-CG50

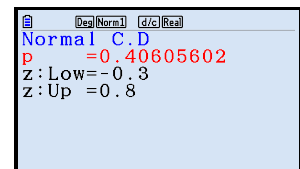
Suppose  $X$  is normally distributed with mean 40 and standard deviation 10.

To find  $P(37 < X < 48)$ , first select **Statistics** from the Main Menu.

Press **F5** (**DIST**), **F1** (**NORM**), **F2** (**Ncd**), and set up the screen as shown.



Scroll down to **Execute**, and press **EXE** to display the result.



So,  $P(37 < X < 48) \approx 0.406$ .

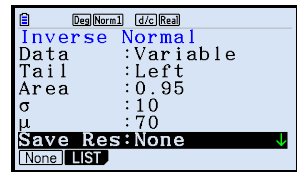
## CHAPTER 28 - CALCULATING QUANTILES

### Casio fx-CG50

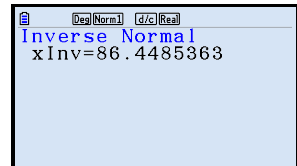
Suppose  $X$  is normally distributed with mean 70 and standard deviation 10.

To find  $k$  such that  $P(X \leq k) = 0.95$ , select **Statistics** from the Main Menu.

Press **F5** (**DIST**), **F1** (**NORM**), **F3** (**InvN**), and set up the screen as shown.



Scroll down to **Execute**, and press **EXE** to display the result.



So,  $k \approx 86.45$ .